

Salgon International Gollege Department of Mathematics and Science Semester 2, 2022 Year 11 ATAR Mathematics Methods Test 5 (Sequences and series)

Section One (Calculator Free)

Time Allowed:	30 minutes
Student's Nam	e: Chu holy . : Diza

Total availale mark: 33

Question 1

(9 marks)

(a) Given an arithmetic sequence has the terms $T_{\rm s}=9$ and $T_{\rm g}=15$ calculate

(6 marks)

(i) the general equation for T_n

(ii) the recursive equation for $T_{\rm H}$

(b) Express the recurring decimal $0.\overline{27} = 0.2727...$ as a sum to infinity and hence express it as a rational number (3 marks)

(8 marks)

(a) The tenth term of an arithmetic sequence is 98 and the sixteenth term is 80. Determine the sum of the first 20 terms of the sequence. (4 marks)

(b) The first two terms of a geometric sequence are 3×10^{-4} and 6×10^{-6} . Calculate the fifth term of the sequence, giving your answer in scientific notation. (4 marks)

(7 marks)

(a) State whether the following sequences are Arithmetic or Geometric and state the 6th term of the sequence.

i. 2, -4, 8, -16

(2 marks)

ii. a, ax², ax⁴

(2 marks)

(b) Consider the sequence, -4, 1, 6, ...

i. State the recursive definition for the sequence.

(2 marks)

ii. Which term is equal to 56?

(1 marks)

(5 marks)

The sum of the first n terms of an arithmetic progression are given by

 $S_n = 3n(n-1) - 18n$

Determine:

a. T1.

(1 mark)

b. The common difference.

(2 marks)

c. Determine n if $S_n = 0$.

(2 marks)

Question 5 (4 marks)

A geometric sequence is described by the rule $Tn = 5x3^n$, where $n = 1, 2, 3, 4, \ldots$ Find the first three terms of the sequence. Hence state the recursive rule for this sequence.

End of Section One



Saigon International College Department of Mathematics and Science Semester 2, 2022

Year 11 ATAR Mathematics Methods Test 5

(Sequence and series)

(6% weighting for the Unit 1 and Unit 2)
Section Two (Calculator Assumed)

Time Allowed: 55 minutes

Total available mark: 52

Question 6

(6 marks)

(a) In a given arithmetic sequence $T_1 = 7$ and $T_{20} = 45$. Evaluate S_{20}

(3 marks)

(b) In a given geometric sequence $T_1 = 256$ and $T_9 = 1$. Evaluate S_{10}

(3 marks)

(6 marks)

The table shows the compound growth of an initial investment of \$5000 at the end of each successive year.

Principal (\$)	Annual Interest (\$)
5300.00	300.00
5618.00	318.00
5955.08	337.08
6312.38	357.30
6691.13	378.74
	5300.00 5618.00 5955.08 6312.38

(a) Given T_1 is the start of 2018, state the recursive formula for

(4 marks)

(i) the value of the principal at the end of successive years

(ii) the annual interest earned at the end of successive years

(b) calculate the value of the principal at the end of 2030

(2 marks)

a. A sequence is defined by $A_{n+1} = 3^n - 2$ where $A_1 = -1$. Determine A_2 and A_3 . (2 marks)

b. $T_{n+3} = T_{n+2} + T_{n+1} - T_n + 2$ produces a sequence where $T_2 = 1$, $T_3 = 2$, $T_4 = 3$. Determine T_1 and T_5 . (2 marks)

b. A sequence defined explicitly by $B_n = 2^{n-2}$. Write the recursive definition for the sequence.

(2 marks)

- c. The 10th term of an arithmetic progression is 28 and the 7th term is 19.
 - i. Calculate the first three terms of the progression.

(3 marks)

it. Which term in the sequence is 82?

(1 mark)

(7 marks)

(a) Determine the first negative term of the sequence 99, 95, 91.

(3 marks).

(b) A couple gave gifts to various charities over a number of years. Over the last twelve year period they gave gifts annually, increasing in the form of an arithmetic sequence, starting with \$200 twelve years ago, increasing to \$1201 in the twelfth year.

Determine how much they donated over the twelve years.

(4 marks) .

(10 marks)

a. Determine the sum of the following series. $35+32+29+\ldots+5$

(2 marks)

b. How many terms of the series -3 +5 +13 + . . . must be added to give a sum of 261? .(2 marks)

c. Three numbers form a geometric sequence. Their sum is 21 and their product is 64.

Determine the three numbers.. (3 marks)

d. In a converging geometric series $S_{\infty} = \frac{3}{2}$ and the sum of the first 3 terms is $\frac{14}{9}$.

Determine the value of r, the constant ratio. (3 marks)

Question 11 (5 marks)

Jenny has 6 weeks to train from the City to Surf Marathon.

a. Jenny's training schedule demands that she runs a total of 8000 km. Each week she plans to run a constant number of kilometers further then the week before. If she starts by running 100 km in the first week, how much further she run each week in irder to complete 800km planned in the schedule? (3 marks)

- b. Jenny decides she can also increase her fitness level by skipping. She starts with 60 skips a minute and wants to increase the rate by 5% each week.
 - i. How many skips per minutes is she skipping during the last week before the Marathon? (i.e Week 6)
 (1 mark)

ii. How many weeks would it take Jenny to be able to skip at over double her initial rate? (1 mark)

\$1,000,000 is invested in an account that pays interest at a rate of 5% per annum compounded annually. Let B_n be the account balance at the end of n years/.

a. Find the general rule for the account balance at the end of n years. (2 marks)

Find the growth in the account balance in the first 10 years. Hence, find the average percentage growth rate in the first 10 years.

c. Calculate the average percentage growth rate in the first 20 years. (2 marks)

d. Give an explanation for the different answers in the parts((b) and (c). (2 marks)